

PUBLISHER CORRECTION

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# Publisher Correction to: Three-dimensional tumor growth in time-varying chemical fields: a modeling framework and theoretical study

Markos Antonopoulos\*, Dimitra Dionysiou, Georgios Stamatakos and Nikolaos Uzunoglu

## Correction to: BMC Bioinformatics

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Following publication of the original article [1], the authors noticed that the following errors were introduced by pdf/html formatting issues. The original article has been corrected. The publisher apologizes to the authors and readers for these errors.

### Page 9, first column:

The paragraph

“-  $o_b(A)$ : sec) by the local vascular network within/sec) by the local vascular network within  $A$  during the previous time interval  $t - \Delta\tau \rightarrow t$ ”

Should be replaced with

“-  $o_b(A)$ : Oxygen supply rate (pmols/sec) by the local vascular network within  $A$  during the previous time interval  $t - \Delta\tau \rightarrow t$ ”

In the subsequent paragraph, i.e. the paragraph starting with the phrase “-  $gl_b(A)$ : Glucose supply rate ...”

the phrase “interval- $\Delta\tau \rightarrow t$ ” should be replaced with “interval  $t - \Delta\tau \rightarrow t$ ”

### Page 11, second column:

The equation  $\beta \geq 1 - \frac{6O_{av}}{l_t(A)K_{ATP}\Delta\tau} \equiv \beta_-$  should be  $\beta \geq 1 - \frac{6O_{av}}{l_t(A)K_{ATP}\Delta\tau} \equiv \underline{\beta}$ .

In the subsequent sentence, i.e. “Since  $a_o(\beta)$  is increasing,  $\beta_-$  is actually ...” the “ $\beta_-$ ” should be “ $\underline{\beta}$ ”.

In the subsequent paragraph (first bullet point), in the sentence “If  $\beta_- > \beta_2$ , we have that ...” the “ $\beta_-$ ” should be “ $\underline{\beta}$ ”.

In the subsequent paragraph (second bullet point), i.e. “If  $\beta_- \leq \beta_2$ , we have that for each  $\beta \in [\max(\beta_-, \beta_1), \beta_2]$  it holds that  $a_o(\beta) \geq 0$ .” all occurrences of “ $\beta_-$ ” should be “ $\underline{\beta}$ ”.

In paragraph 11a, first line, “ $a_o(\beta)$ ” should be “ $a_{gl}(\beta)$ ”.

### Page 12, first column:

In the sentence “Case 2.2.1. If  $\beta > \beta_2$  or  $\bar{\beta} < \beta_1$  or  $\min(\bar{\beta}, \beta_2) < \max(\beta_-, \beta_1)$ , the analysis above implies that ...” the inequality  $\beta > \beta_2$  should be  $\underline{\beta} > \beta_2$  and the inequality  $\min(\bar{\beta}, \beta_2) < \max(\beta_-, \beta_1)$  should be  $\min(\bar{\beta}, \beta_2) < \max(\underline{\beta}, \beta_1)$ .

In the sentence “Case 2.2.2. If  $\beta \leq \beta_2$ ,  $\bar{\beta} \geq \beta_1$  and  $\min(\bar{\beta}, \beta_2) \geq \max(\beta_-, \beta_1)$ ...” the inequality  $\beta \leq \beta_2$  should be  $\underline{\beta} \leq \beta_2$  and the inequality  $\min(\bar{\beta}, \beta_2) \geq \max(\beta_-, \beta_1)$  should be  $\min(\bar{\beta}, \beta_2) \geq \max(\underline{\beta}, \beta_1)$ .

In the same paragraph, the mathematical expression  $\beta \in [\max(\beta_-, \beta_1), \min(\bar{\beta}, \beta_2)]$  should be  $\beta \in [\max(\underline{\beta}, \beta_1), \min(\bar{\beta}, \beta_2)]$

### Page 12, second column:

In the sentence “Again, we pick a random  $\tilde{\beta}$  in  $[\max(\beta_-, \beta_1), \min(\bar{\beta}, \beta_2)]$ .” the mathematical expression  $[\max(\beta_-, \beta_1), \min(\bar{\beta}, \beta_2)]$  should be  $[\max(\underline{\beta}, \beta_1), \min(\bar{\beta}, \beta_2)]$

### Page 14, second column:

The equations

$$\begin{aligned} ob \max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))v_r \\ &+ sw_t(A) f_e(l_t(A), nc_t(A), \\ &nn_t(A))v_e) \cdot ob \max_t(A) \end{aligned}$$

$$\begin{aligned} glb \max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))v_r \\ &+ sw_t(A) f_e(l_t(A), nc_t(A), \\ &nn_t(A))v_e) \cdot glb \max_t(A) \end{aligned}$$

\* Correspondence: [markosan@central.ntua.gr](mailto:markosan@central.ntua.gr)

Institute of Communication and Computer Systems, National Technical University of Athens, Athens, Greece



should be

$$\begin{aligned}
 o\_b\_max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))v_r \\
 &\quad +sw_t(A) f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))v_e) \cdot o\_b\_max_t(A) \\
 gl\_b\_max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))v_r \\
 &\quad +sw_t(A)f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))v_e) \cdot gl\_b\_max_t(A).
 \end{aligned}$$

The equations

$$\begin{aligned}
 ob \ max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))r_3v_r \\
 &\quad +sw_t(A) f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))r_4v_e) \cdot ob \ max_t(A) \\
 glb \ max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))r_3v_r \\
 &\quad +sw_t(A)f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))r_4v_e) \cdot glb \ max_t(A)
 \end{aligned}$$

should be

$$\begin{aligned}
 o\_b\_max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))r_3v_r \\
 &\quad +sw_t(A) f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))r_4v_e) \cdot o\_b\_max_t(A) \\
 gl\_b\_max_{t+\Delta\tau}(A) &= (1-f_r(l_t(A), nc_t(A))r_3v_r \\
 &\quad +sw_t(A)f_e(l_t(A), nc_t(A), \\
 &\quad nn_t(A))r_4v_e) \cdot gl\_b\_max_t(A)
 \end{aligned}$$

**Page 15, first column:**

The equations

$$\begin{aligned}
 ob \ max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot ob \ max_t(A) \\
 glb \ max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot glb \ max_t(A)
 \end{aligned}$$

should be

$$\begin{aligned}
 o\_b\_max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot o\_b\_max_t(A) \\
 gl\_b\_max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot gl\_b\_max_t(A)
 \end{aligned}$$

**Page 15, second column:**

The equations

$$\begin{aligned}
 ob \ max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot ob \ max_t(A) \\
 glb \ max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot glb \ max_t(A)
 \end{aligned}$$

Should be

$$\begin{aligned}
 o\_b\_max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot o\_b\_max_t(A) \\
 gl\_b\_max_{t+\Delta\tau}(A) &= \left(1 - \frac{l_t(A) + nc_t(A)}{M} r_3 v_r \right. \\
 &\quad \left. + sw_t(A) \frac{M - l_t(A) - nc_t(A) - nn_t(A)}{M} r_4 v_e \right) \\
 &\quad \cdot gl\_b\_max_t(A)
 \end{aligned}$$

The second equation appearing in this column, i.e.

$$\begin{aligned}
 gl\_b_{t+\Delta\tau}(A) &= B_{o\_b\_max_{t+\Delta\tau}(A)}( gl\_b_t(A) \\
 &\quad + r_2((\overline{gl}_0 - gl_t(A)) / \Delta\tau) )
 \end{aligned}$$

Should be

$$\begin{aligned}
 gl\_b_{t+\Delta\tau}(A) &= B_{gl\_b\_max_{t+\Delta\tau}(A)}( gl\_b_t(A) \\
 &\quad + r_2((\overline{gl}_0 - gl_t(A)) / \Delta\tau) )
 \end{aligned}$$

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**Reference**

1. Antonopoulos M, Dionysiou D, Stamatakis G, Uzunoglu N. Three-dimensional tumor growth in time-varying chemical fields: a modeling framework and theoretical study. BMC Bioinformatics. 2019;20:Article number: 442.